

Effects of Gravity on Supercritical Water Oxidation (SCWO) Processes

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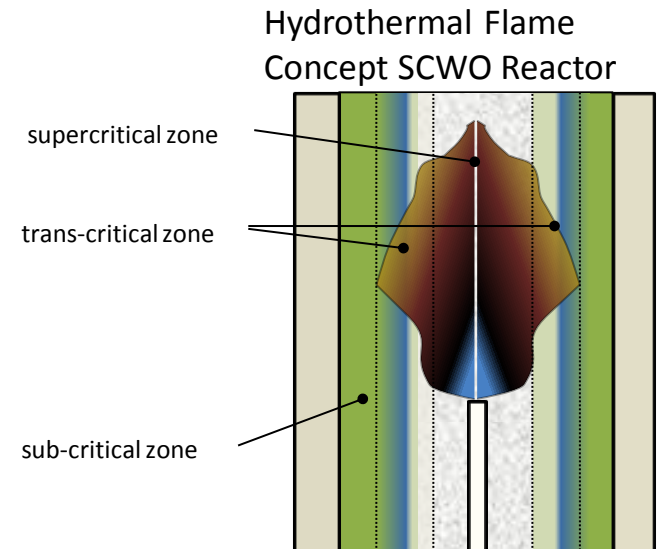
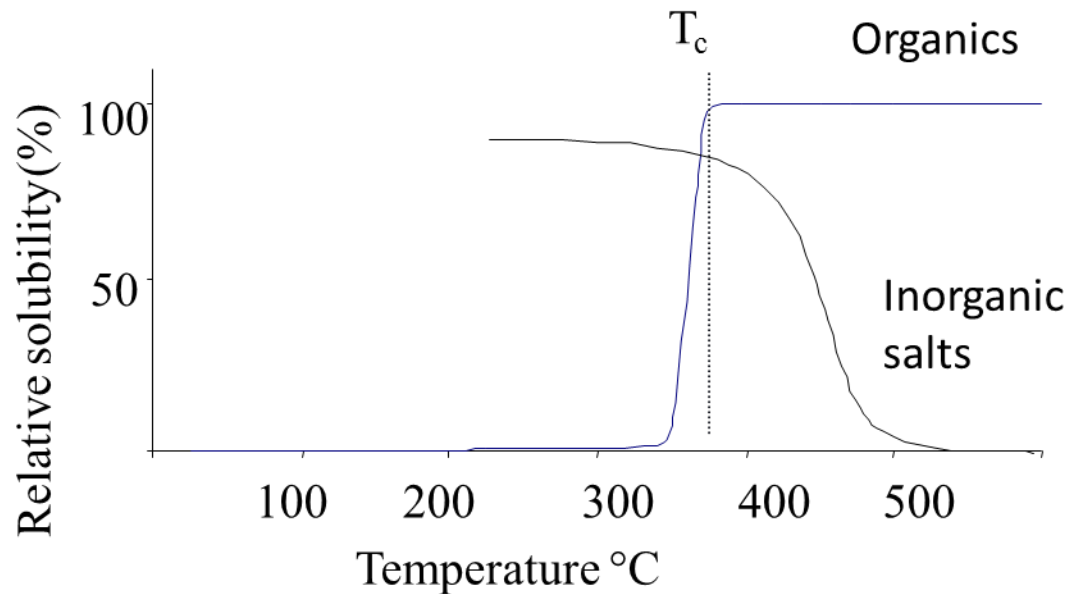
Michael Hicks

NASA John H. Glenn Research Center

Motivation and Application

Precursor study to the investigation of supercritical water oxidation (SCWO)

Dissolve inorganic precipitates generated during SCWO in a subcritical shroud



Objectives

- Characterize the hydrodynamics of supercritical water jets
- Identify the jet injection conditions leading to laminar and turbulent regimes
- Assess the effects of buoyancy on the jet behavior

$Re \sim \text{Momentum/Viscous}$

$$Re = \frac{\rho U d}{\mu}$$

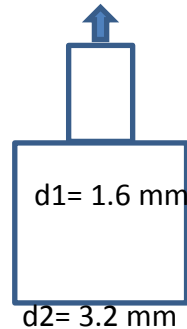
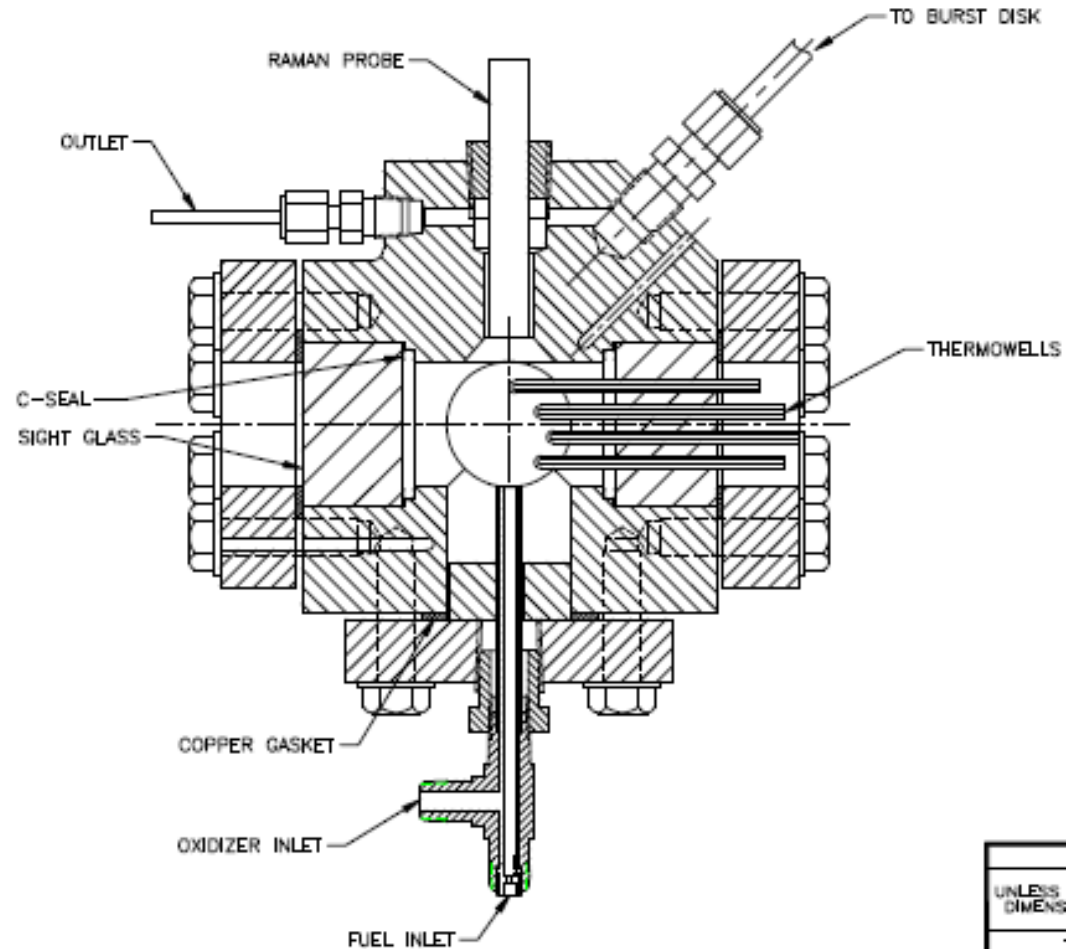
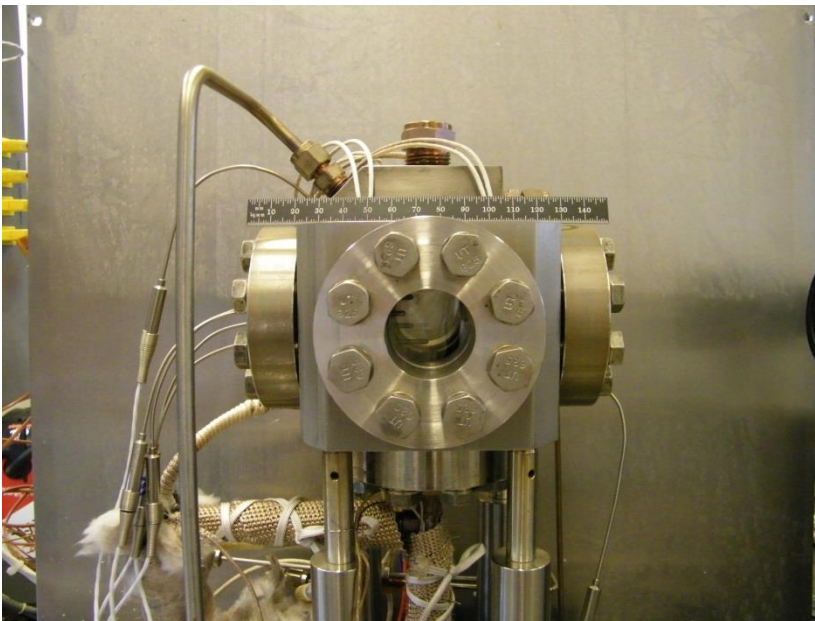
$F \sim \text{Momentum/Buoyancy}$

$$F = \frac{U}{\left(\frac{\Delta\rho}{\rho} g d\right)^{1/2}}$$

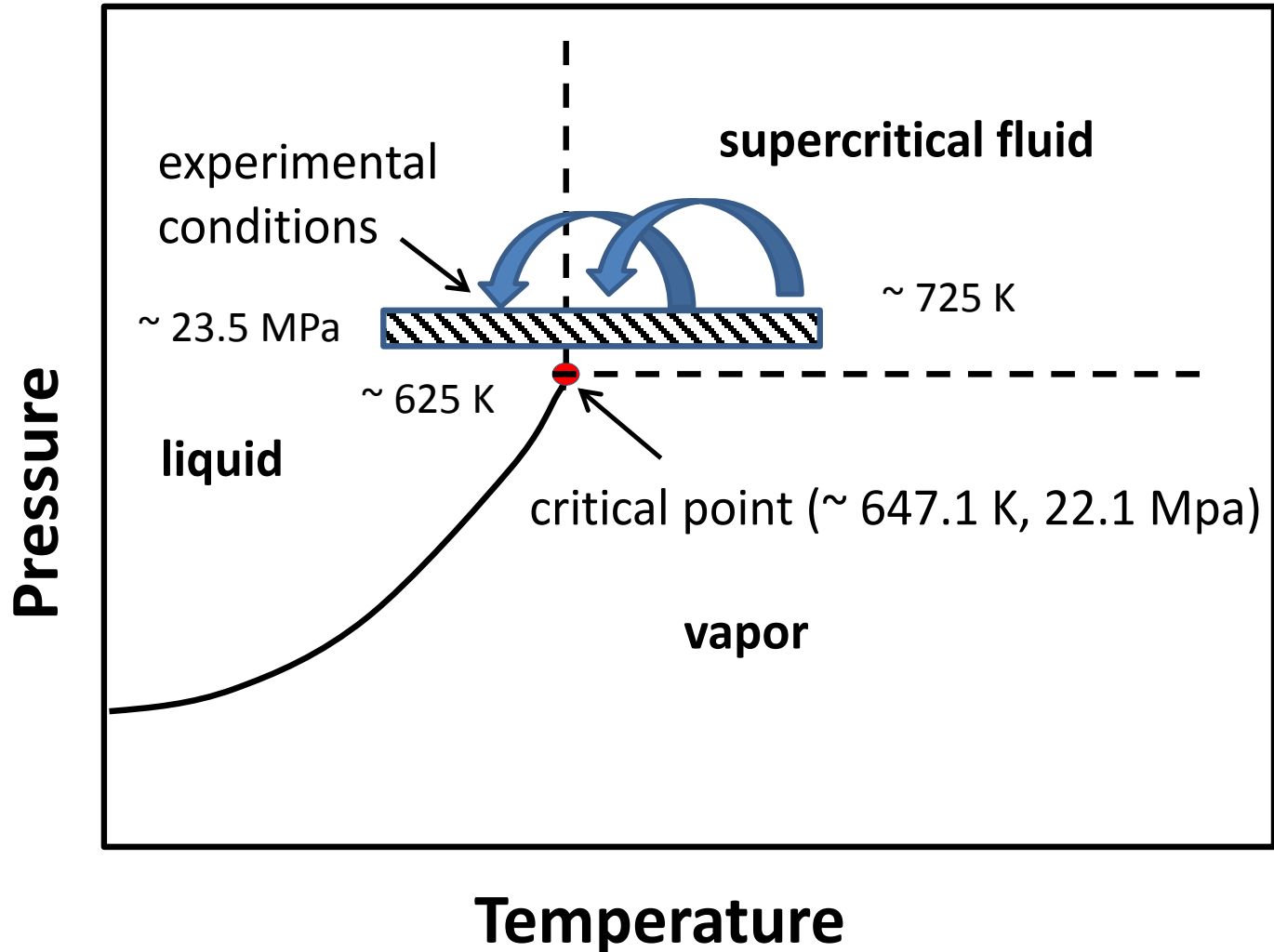
$Gr \sim \text{Buoyancy/Viscous}$

$$Gr = \left(\frac{Re}{F}\right)^2$$

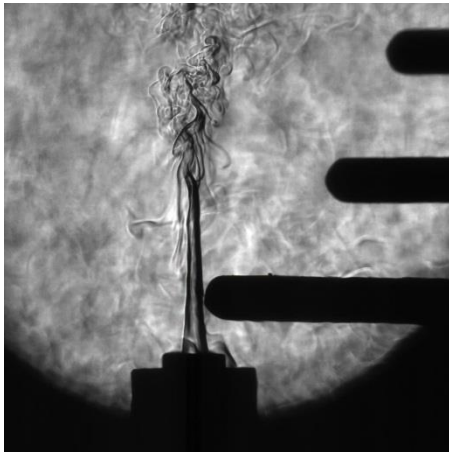
SUPERCritical WATER TEST CELL



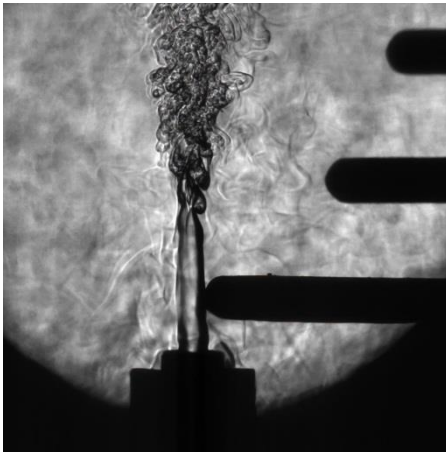
Experimental Conditions



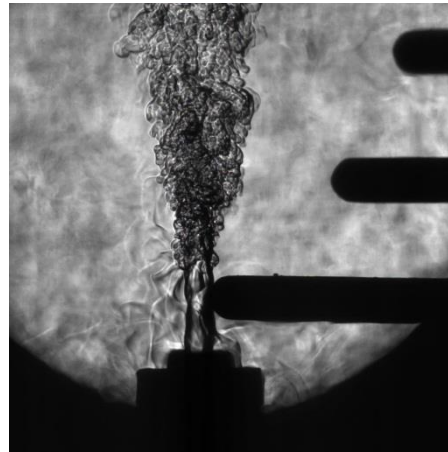
Supercritical Jet Injected into Supercritical Water



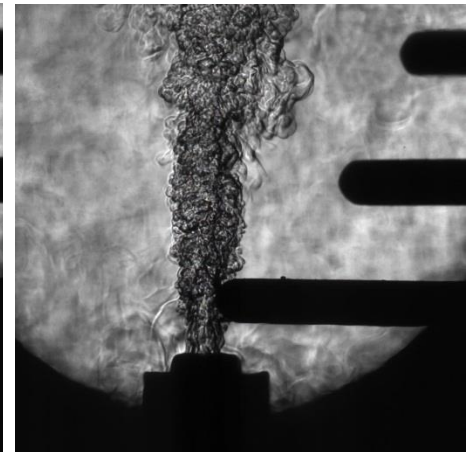
$Re = 448$
 $F = 1.37$



$Re = 1330$
 $F = 3.81$



$Re = 1780$
 $F = 5.03$

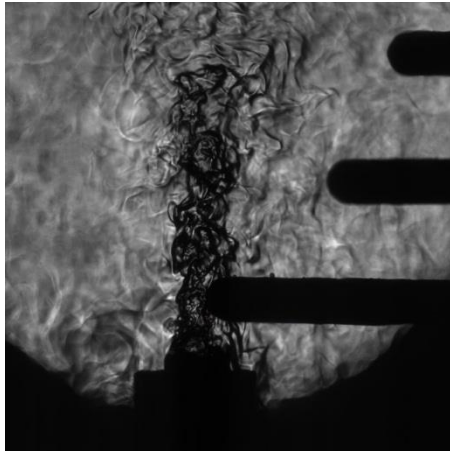


$Re = 2680$
 $F = 7.31$

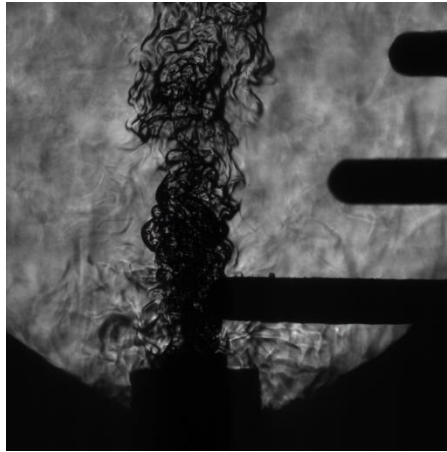
As Re increases, jet transitions from mostly laminar to turbulent

Classical Reynolds number transition to turbulence of jets

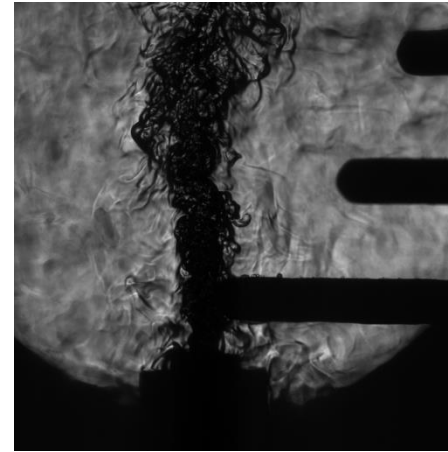
Supercritical Jet Injected into Subcritical Water



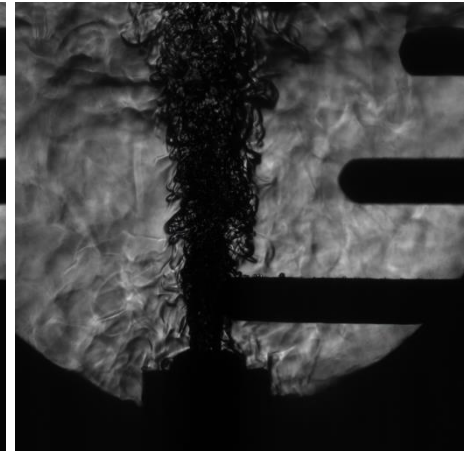
$Re = 471$
 $F = 0.5$



$Re = 943$
 $F = 1.0$



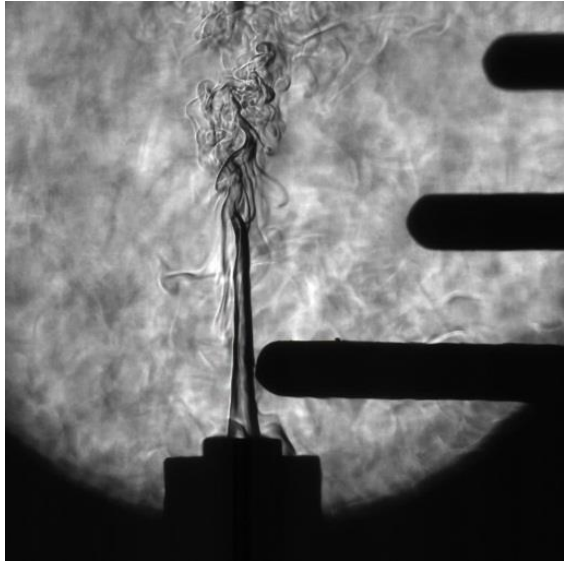
$Re = 1890$
 $F = 2.0$



$Re = 2830$
 $F = 3.0$

Transition appears to be from turbulent buoyant plume to turbulent buoyant jet

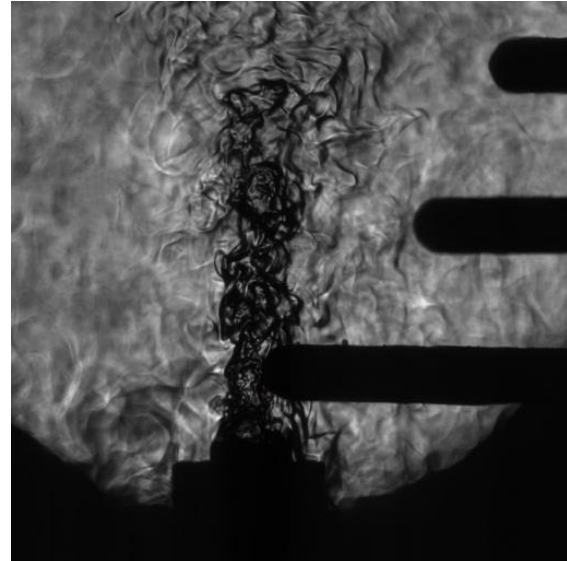
Jet Comparison



Supercritical into supercritical

$Re = 448$

$F = 1.37$



Supercritical into subcritical

$Re = 471$

$F = 0.5$

For similar Reynolds and Froude numbers the character of the two jets is strikingly different.

Property Variations near Critical Point

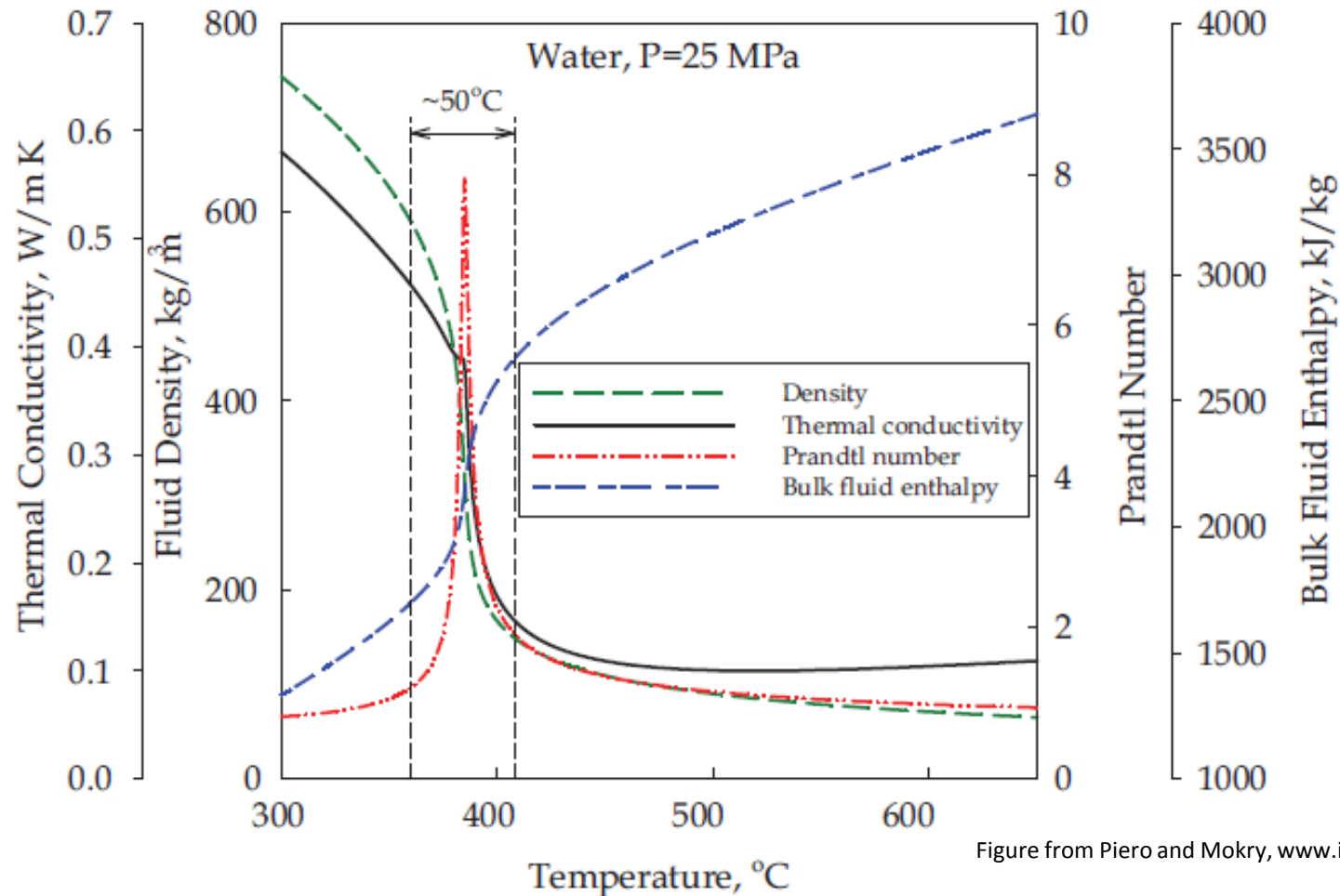


Figure from Piero and Mokry, www.intechopen.com

Influence of compressibility, C_p , λ ?

Vorticity Equation

Consider azimuthal vorticity equation for axisymmetric, variable density with buoyancy flow.

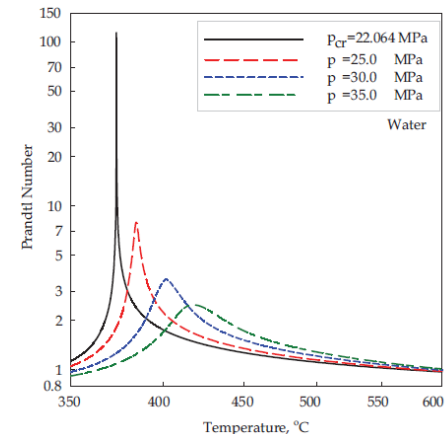
Viscous effects not shown

$$\mathbf{V} = \nabla \times \psi + \nabla \varphi$$

$$\omega = \nabla \times \mathbf{V} = \nabla \times (\nabla \times \psi)$$

$$\nabla \cdot \mathbf{V} = \nabla^2 \varphi$$

$$\underbrace{\frac{D\omega}{Dt} - \omega \frac{v_r}{r}}_{\text{Vortex Stretching}} + \underbrace{\omega (\nabla \cdot \mathbf{V})}_{\substack{\text{Compressibility} \\ \sim M^2}} = \underbrace{\frac{1}{\rho^2} \left(\frac{\partial \rho}{\partial r} \frac{\partial p}{\partial x} - \frac{\partial p}{\partial r} \frac{\partial \rho}{\partial x} \right)}_{\substack{\text{Baroclinic} \\ \sim \text{Pr}}} - \underbrace{\frac{g}{\rho} \frac{\partial \rho}{\partial r}}_{\substack{\text{Buoyancy} \\ \sim \text{Pr}/F^2}}$$



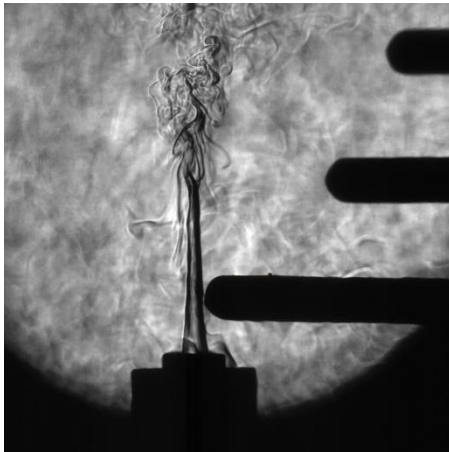
- Prandtl number ($\text{Pr} = \mu C_p / \lambda = \delta_v / \delta_T$) comes in because thermal mixing layer thickness can be much different (thinner) than velocity shear layer

$$\text{Note } \text{Pr}/F^2 \sim \text{Ra}/\text{Re}^2$$

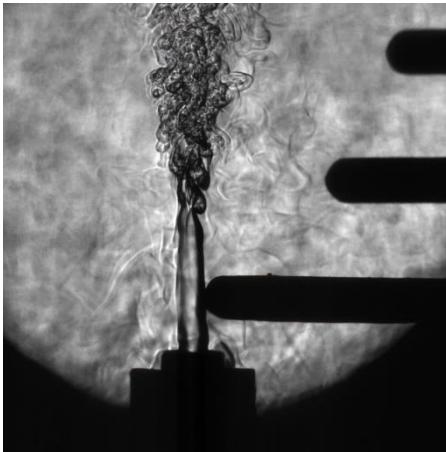
- $M^2 \ll 1$ for the conditions of the experiment. It can be large very close to the critical point (speed of sound $\rightarrow 0$)

Supercritical Jet Injected into Supercritical Water

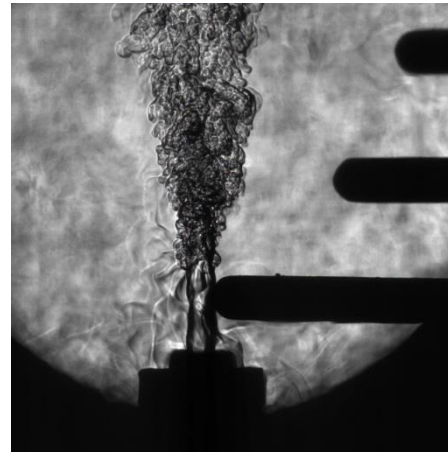
Transition from Buoyant Laminar Jet to Buoyant Turbulent Jet



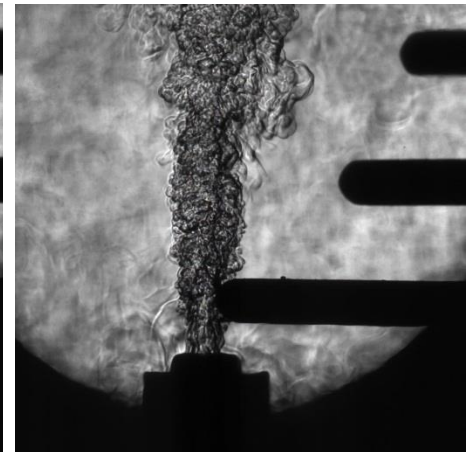
$Re = 448$
 $Pr/F^2 = 1.4$



$Re = 1330$
 $Pr/F^2 = 0.2$



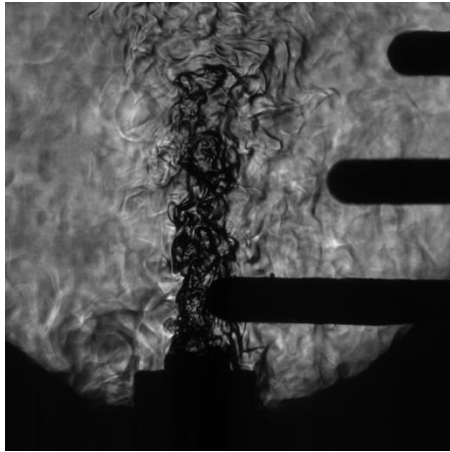
$Re = 1780$
 $Pr/F^2 = 0.11$



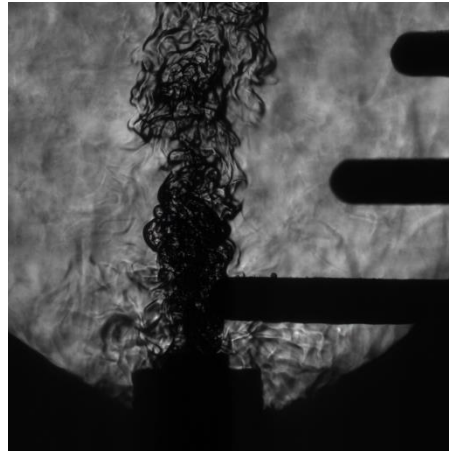
$Re = 2680$
 $Pr/F^2 = 0.05$

Supercritical Jet into Subcritical Water

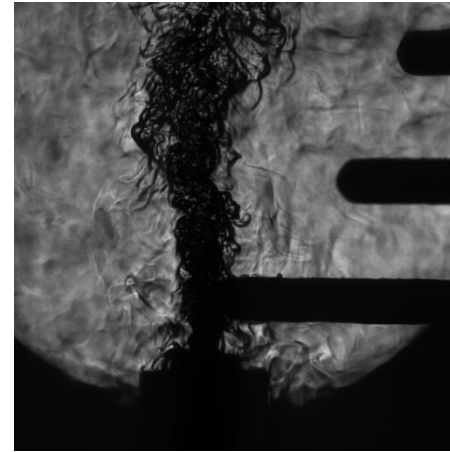
Transition from Buoyant Turbulent Plume to Buoyant Turbulent Jet



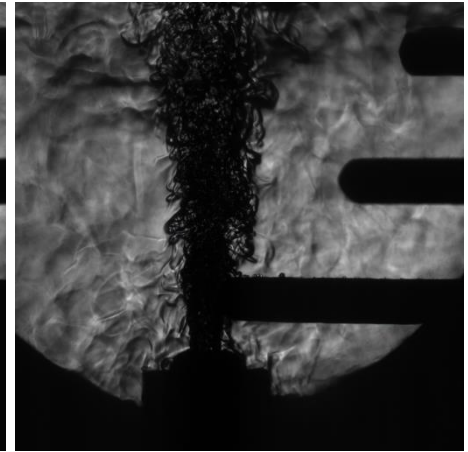
$Re = 471$
 $Pr/F^2 = 56$



$Re = 943$
 $Pr/F^2 = 14$

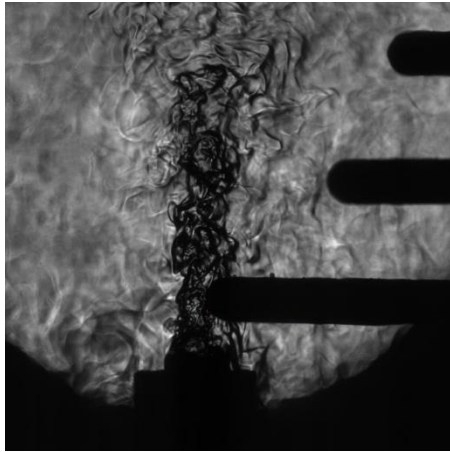


$Re = 1890$
 $Pr/F^2 = 3.5$

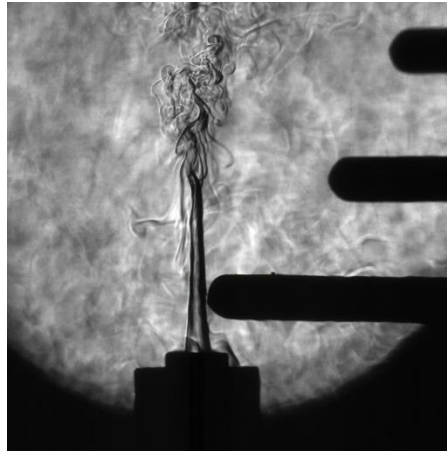


$Re = 2830$
 $Pr/F^2 = 1.6$

Findings



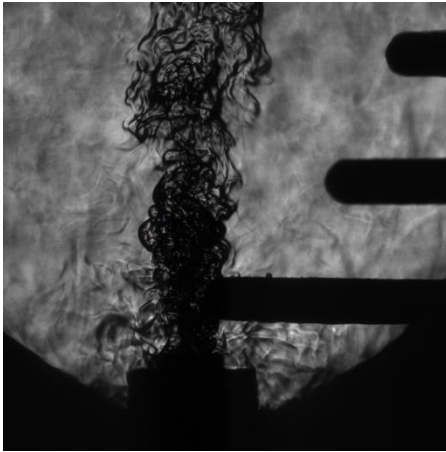
$Re = 471$
 $Pr/F^2 = 56$



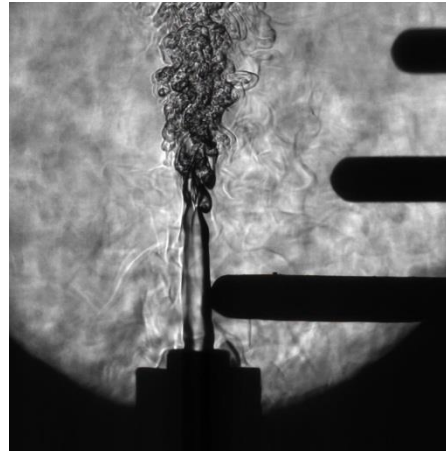
$Re = 448$
 $Pr/F^2 = 1.4$

At low Reynolds number, the parameter Pr/F^2 controls the laminar/turbulent nature of the jet. For values of the parameter $\gg 1$, the jet is turbulent due to strong buoyancy effect.

Findings (contd)



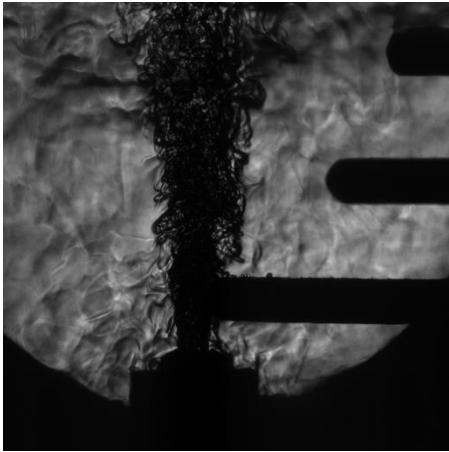
$Re = 943$
 $Pr/F^2 = 14$



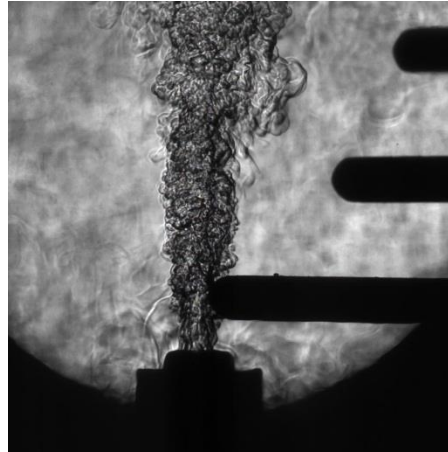
$Re = 1330$
 $Pr/F^2 = 0.2$

At intermediate Reynolds number the situation is similar to the low Reynolds number case.

Findings (contd 2)



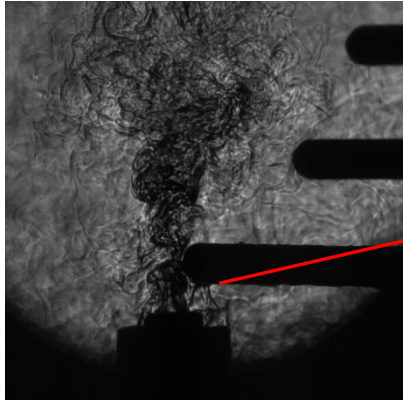
$Re = 2830$
 $Pr/F^2 = 1.6$



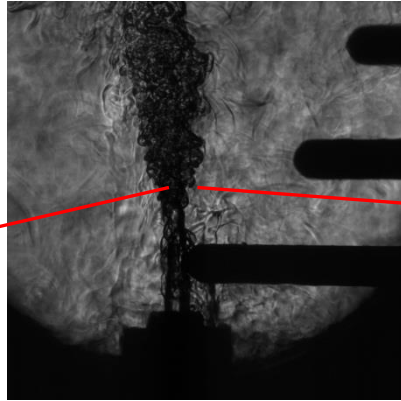
$Re = 2680$
 $Pr/F^2 = 0.05$

At large Reynolds numbers
(> 2000), the jet is
turbulent.

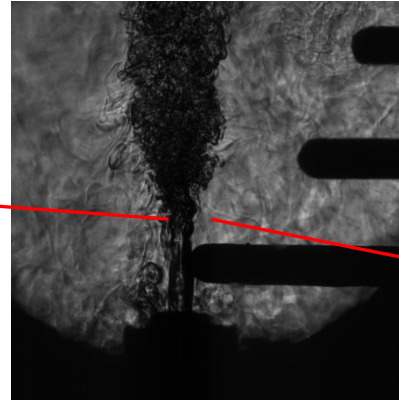
Supercritical Jet (~450 C) Injected into Transcritical Water (~380 C)



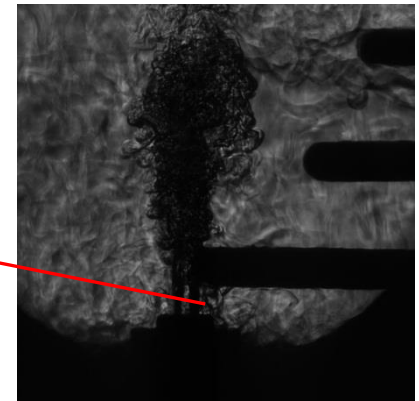
Re = 466
 $Pr/F^2 = 7$



Re = 935
 $Pr/F^2 = 1.2$



Re = 1400
 $Pr/F^2 = 0.6$



Re = 1880
 $Pr/F^2 = 0.4$

Note appearance of laminar length as flow transitions from plume to jet behavior

Summary

- Behavior of supercritical water jets injected into subcritical and supercritical was studied
- The laminar/turbulent nature of the jet under gravitational conditions depends upon the Reynolds number of injection and the parameter $\text{Prandtl number}/(\text{Froude number})^2$
- Compressibility may be important near the critical point but it is not clear it can be separated from gravity effects on the ground

Acknowledgments

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